

Ratio Games

11-1



Overview

- Ratio Game Examples
- Using an Appropriate Ratio Metric
- Using Relative Performance Enhancement
- Ratio Games with Percentages
- Ratio Games Guidelines
- Numerical Conditions for Ratio Games

11-2

Case Study 11.1: 6502 vs. 8080

| Bench- mark | System | |
|----------------|--------|-------|
| | 6502 | 8080 |
| Block | 41.16 | 51.50 |
| Sieve | 63.17 | 48.08 |
| Sum | 104.33 | 99.58 |
| Avg | 52.17 | 49.79 |

1. Ratio of Totals

- Conclusion: 6502 is worse. It takes 4.7% more time than 8080.

11-3

6502 vs. 8080 (Cont)

2. 6502 as the base:

| System | |
|--------|------|
| 6502 | 8080 |
| 1.00 | 1.25 |
| 1.00 | 0.76 |
| 2.00 | 2.01 |
| 1.00 | 1.01 |

3. 8080 as the base:

| System | |
|--------|------|
| 6502 | 8080 |
| 0.80 | 1.00 |
| 1.31 | 1.00 |
| 2.11 | 2.00 |
| 1.06 | 1.00 |

1. Ratio of Totals: 6502 is worse. It takes 4.7% more time than 8080.
2. With 6502 as a base: 6502 is better. It takes 1% less time than 8080.
3. With 8080 as a base: 6502 is worse. It takes 6% more time.

11-4

Case Study 11.2: RISC vs. CISC

| Benchmark | Processor | | | | |
|--------------------|-----------|---------|------------|-----------|---------|
| | RISC-I | Z8002 | VAX-11/780 | PDP-11/70 | C/70 |
| E-String Search | 144 | 130 | 101 | 115 | 101 |
| F-Bit Test | 120 | 180 | 144 | 168 | 120 |
| H-Linked List | 176 | 141 | 211 | 299 | 141 |
| K-Bit Matrix | 288 | 374 | 288 | 374 | 317 |
| I-Quick Sort | 992 | 1091 | 893 | 1091 | 893 |
| Ackermann(3,6) | 144 | 302 | 72 | 86 | 86 |
| Recursive Qsort | 2736 | 1368 | 1368 | 1642 | 1642 |
| Puzzle (Subscript) | 2796 | 1398 | 1398 | 1398 | 1678 |
| Puzzle (Pointer) | 752 | 602 | 451 | 376 | 376 |
| SED (Batch Editor) | 17,720 | 17,720 | 10,632 | 8860 | 8860 |
| Towers Hanoi (18) | 96 | 240 | 77 | 96 | 67 |
| Sum | 25,964 | 23,546 | 15,635 | 14,505 | 14,281 |
| Average | 2360.36 | 2140.55 | 1421.36 | 1318.64 | 1298.27 |

- Conclusion: RISC-I has the largest code size. The second processor Z8002 requires 9% less code than RISC-I.

11-5

RISC vs. CISC (Cont)

| Benchmark | Processor | | | | |
|--------------------|-----------|-------|------------|-----------|------|
| | RISC-I | Z8002 | VAX-11/780 | PDP-11/70 | C/70 |
| E-String Search | 1.00 | 0.90 | 0.70 | 0.80 | 0.70 |
| F-Bit Test | 1.00 | 1.50 | 1.20 | 1.40 | 1.00 |
| H-Linked List | 1.00 | 0.80 | 1.20 | 1.70 | 0.80 |
| K-Bit Matrix | 1.00 | 1.30 | 1.00 | 1.30 | 1.10 |
| I-Quick Sort | 1.00 | 1.10 | 0.90 | 1.10 | 0.90 |
| Ackermann(3,6) | 1.00 | 2.10 | 0.50 | 0.60 | 0.60 |
| Recursive Qsort | 1.00 | 0.50 | 0.50 | 0.60 | 0.60 |
| Puzzle (Subscript) | 1.00 | 0.50 | 0.50 | 0.50 | 0.60 |
| Puzzle (Pointer) | 1.00 | 0.80 | 0.60 | 0.50 | 0.50 |
| SED (Batch Editor) | 1.00 | 1.00 | 0.60 | 0.50 | 0.50 |
| Towers Hanoi (18) | 1.00 | 2.50 | 0.80 | 1.00 | 0.70 |
| sum 11.00 | 13.00 | 8.50 | 9.99 | 8.00 | |
| Average | 1.00 | 1.18 | 0.77 | 0.91 | 0.73 |

- Conclusion: Z8002 has the largest code size and that it takes 18% more code than RISC-I. [Peterson and Sequin 1982]

11-6

Using an Appropriate Ratio Metric

Example:

| Network | Throughput | Response |
|---------|------------|----------|
| A | 10 | 2 |
| B | 4 | 1 |

| System | Throughput | Response | Power |
|--------|------------|----------|-------|
| A | 10 | 2 | 5 |
| B | 4 | 1 | 4 |

1. Throughput: A is better
2. Response Time: A is worse
3. Power: A is better

11-7

Using Relative Performance Enhancement

Example: Two floating point accelerators

| Alternative | Without | With |
|-------------|---------|------|
| A on X | 2 | 4 |
| B on Y | 3 | 5 |

| Alternative | Without | With | Ratio |
|-------------|---------|------|-------|
| A on X | 2 | 4 | 2.00 |
| B on Y | 3 | 5 | 1.66 |

- Problem: Incomparable bases. Need to try both on the same machine

11-8

Ratio Games with Percentages

Example: Tests on two systems

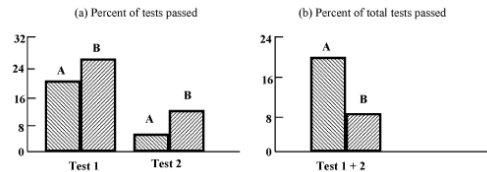
| System A: | Test | Total | Pass | % Pass |
|-----------|-------|-------|------|--------|
| | 1 | 300 | 60 | 20% |
| | 2 | 50 | 2 | 4% |
| | Total | 350 | 62 | 20.6% |

| System B: | Test | Total | Pass | % Pass |
|-----------|-------|-------|------|--------|
| | 1 | 32 | 8 | 25% |
| | 2 | 500 | 40 | 8% |
| | Total | 532 | 48 | 9% |

1. System B is better on *both* systems
2. System A is better overall.

11-9

Percentages (Cont)



Other Misuses of Percentages:

- > 1000% sounds more impressive than 11-time. Particularly if the performance before and after the improvement are both small
- > Small sample sizes disguised in percentages
- > Base = Initial. 400% reduction in prices \Rightarrow Base = Final

11-10

Ratio Games Guidelines

1. If one system is better on *all* benchmarks, *contradicting* conclusions can not be drawn by any ratio game technique

| Bench- mark | System | |
|----------------|--------|------|
| | A | B |
| I | 0.50 | 1.00 |
| J | 1.00 | 1.50 |
| Average | 0.75 | 1.25 |

| Bench- mark | System | | Bench- mark | System | |
|----------------|--------|------|----------------|--------|------|
| | A | B | | A | B |
| I | 1.00 | 2.00 | I | 0.50 | 1.00 |
| J | 1.00 | 1.50 | J | 0.67 | 1.00 |
| Average | 1.00 | 1.75 | Average | 0.58 | 1.00 |

11-11

Guidelines (cont)

2. Even if one system is better than the other on all benchmarks, a better *relative* performance can be shown by selecting appropriate base.
 - > In the previous example, System A is 40% better than System B using raw data, 43% better using system A as a base, and 42% better using System B as a base.
3. If a system is better on some benchmarks and worse on others, contradicting conclusions can be drawn in some cases. Not in all cases.
4. If the performance metric is an LB metric, it is better to use your system as the base
5. If the performance metric is an HB metric, it is better to use your opponent as the base
6. Those benchmarks that perform better on your system should be elongated and those that perform worse should be shortened

11-12

Numerical Conditions for Ratio Games

Raw Data:

| Bench- mark | System | |
|----------------|-----------------|-------------------|
| | A | B |
| I | a | ax |
| J | b | by |
| Average | $\frac{a+b}{2}$ | $\frac{ax+by}{2}$ |

A is better than B iff

$$\frac{a+b}{2} > \frac{ax+by}{2}$$

$$y < -\frac{a}{b}x + \frac{a+b}{b}$$

With A as the Base:

| Bench- mark | System | |
|----------------|--------|-----------------|
| | A | B |
| I | 1 | x |
| J | 1 | y |
| Average | 1 | $\frac{x+y}{2}$ |

A is better than B iff

$$\frac{x+y}{2} < 1$$

$$y < 2 - x$$

11-13

Numerical Conditions (Cont)

With B as the base:

| Bench- mark | System | |
|----------------|--|---|
| | A | B |
| I | $\frac{1}{x}$ | 1 |
| J | $\frac{1}{y}$ | 1 |
| Average | $\frac{1}{2} \left(\frac{1}{x} + \frac{1}{y} \right)$ | 1 |

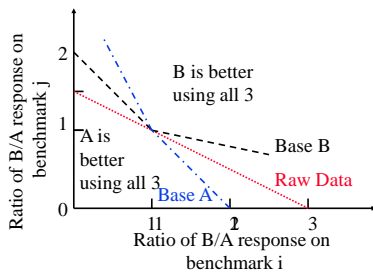
A is better than B iff

$$\frac{1}{2} \left(\frac{1}{x} + \frac{1}{y} \right) > 1$$

$$y < \frac{x}{2x-1}$$

11-14

Numerical Conditions (Cont)



11-15

Summary



- Ratio games arise from use of incomparable bases
- Ratios may be part of the metric
- Relative performance enhancements
- Percentages are ratios
- For HB metrics, it is better to use opponent as the base

11-16