Instructions: Time $\mathbf{2 0}$ minutes. Closed books and notes. No calculators. No questions are allowed.
Q1. Clock, $S$ and $R$ waveforms, one latch and two flip-flops are shown in the figure below. For the latch and the flip-flops, carefully sketch the output waveform, $Q_{i}$, obtained in response to the input waveforms. Assume that the propagation delay of the storage elements is negligible. Initially, all storage elements store 0 .


Q2. A sequential circuit with two D flip-flops $A$ and $B$, two inputs $X$ and $Y$, and one output $Z$ is specified by the following input equations:

$$
D_{A}=X A+X \bar{Y}, \quad D_{B}=X \bar{B}+\bar{X} A, \quad Z=\bar{X} \bar{B}
$$

(a) Draw the logic diagram of the circuit.
(b) Derive the state table.
(c) Derive the state diagram.


| Present State |  | Inputs |  | Next State |  | Output |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{A}$ | $\mathbf{B}$ | $\mathbf{X}$ | $\mathbf{Y}$ | $\mathbf{A}$ | $\mathbf{B}$ | $\mathbf{Z}$ |
| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ |
| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ |
| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{0}$ |
| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ |
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| $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ |
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| $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{0}$ |



