Instructions: Time $\mathbf{2 0}$ minutes. Closed books and notes. No calculators. No questions are allowed.
Q1. Clock and $D$ waveforms, one latch and two flip-flops are shown in the figure below. For the latch and each of the flip-flops, carefully sketch the output waveform, $Q_{i}$, obtained in response to the input waveforms. Assume that the propagation delay of the storage elements is negligible. Initially, all storage elements store 0 .


Q2. A sequential circuit has three D flip-flops $A, B$, and $C$, and one input $X$. The circuit is described by the following input equations:

$$
\begin{gathered}
\boldsymbol{D}_{\boldsymbol{A}}=(\overline{\boldsymbol{B}} \boldsymbol{C}+\overline{\boldsymbol{B}} \overline{\boldsymbol{C}}) \boldsymbol{X}+(\boldsymbol{B} \overline{\boldsymbol{C}}+\overline{\boldsymbol{B}} \overline{\boldsymbol{C}}) \boldsymbol{X} \\
\boldsymbol{D}_{\boldsymbol{B}}=\overline{\boldsymbol{A}} \\
\boldsymbol{D}_{C}=\overline{\boldsymbol{B}}
\end{gathered}
$$

(a) Derive the state table for the circuit.
(b) Derive two state diagram, one for $\mathrm{X}=0$ and the other for $\mathrm{X}=1$.

| Present State |  |  | Next State (X=0) |  |  | Next State (X=1) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | B | C | A | B | C | A | B | C |
| 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 |
| 0 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 1 |
| 0 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 0 |
| 0 | 1 | 1 | 0 | 1 | 0 | 0 | 1 | 0 |
| 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 1 |
| 1 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 1 |
| 1 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |

$X=0$

$\mathrm{X}=1$


